

# A New Top-Down Context-Free Parsing for Syntactic Pattern Recognition

<sup>1</sup>Mehrnoosh Bazrafkan

<sup>1</sup>Department of Computer, Marvdasht Branch, Islamic Azad university, Marvdasht, Iran

Mehrnoosh.bazrafkan@gmail.com

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**Abstract:** The numerous different mathematical methods used to solve pattern recognition snags may be assembled into two universal approaches: the decision-theoretic approach and the syntactic (structural) approach. In this paper, at first syntactic pattern recognition method and formal grammars are described and then has been investigated one of the techniques in syntactic pattern recognition called top – down tabular parser known as Earley’s algorithm Earley’s tabular parser is one of the methods of context -free grammar parsing for syntactic pattern recognition. Earley’s algorithm uses array data structure for implementing, which is the main problem and for this reason takes a lots of time, searching in array and grammar parsing, and wasting lots of memory. In order to solve these problems and most important, the cubic time complexity, in this article, a new algorithm has been introduced, which reduces wasting the memory to zero, with using linked list data structure. Also, with the changes in the implementation and performance of the algorithm, cubic time complexity has transformed into  $O(n \cdot R)$  order.

**Key words:** syntactic pattern recognition, tabular parser, context –free grammar, time complexity, linked list data structure.

## I. INTRODUCTION

Syntactic pattern recognition worries the difficult of determining whether a string  $x$  be

appropriate to a language  $L(G)$  or not, if  $X$  is not deformed, this is called a recognition or a parsing problem. The two tabular parsing methods for context-free language, the cocke-kasami-younger (cky) and the Earley termed. In syntactic pattern recognition, we assume that a pattern can be exemplified by a sequence of primitives and a class of patterns makes a language  $L(G)$ . consider two grammars  $G_1$  and  $G_2$  which represent the class 1 and the class 2, respectively. If a sequence of primitives  $x$  belongs to  $L(G_1)$ ,  $x$  is determined to be a pattern of the class 1. if  $x$  belongs to neither  $L(G_1)$  and  $L(G_2)$ ,  $x$  is rejected, [1]-[3].

In the syntactic approach, formal grammars are used for pattern class representation. The productions of a grammar describe how complex (sub)patterns can be built up from simpler elements. The recognition procedure is based on the concept of formal language parsing. The most fundamental concept is string grammars. They operate on strings of symbols, i.e. words over a finite alphabet. Formal grammars operate on words over finite sets of symbols, [1]-[6].

**Definition :** A formal grammar is a four-tuple  $G = (V_N, V_T, S, P)$  where  $V_N$  is a finite set of nonterminals symbols,  $V_T$  is a finite set of terminal symbols,  $P$  is a finite set of production set or rewriting rules and  $S \in V_N$  is the initial or starting symbol. It is essential that  $V_N \cap V_T = \emptyset$ , the union of  $V_N$  and  $V_T$  is called the vocabulary  $V = V_N \cup V_T$ .

**Definition 2:**

```

9   L[i] = L[i] ∪ {(Y → · γ, i)};
10   end
11   else if (Y ∈ VT and i
≠ n) then begin { * scanner * }
12       if Y = ai+1 then
13           L[i + 1] := L[i +
1] ∪ {(X → αY. β, I)};
14       end
15   else if
Yβ = λ then begin { * completer * }
16       for each (A → δ.Xξ, k) ∈ L[j] do
17           L[i] := L[i] ∪ {(A → δ.Xξ, k)}
18       end
19       end { * of for i * };
20   if (no new item has been generated
in L[i] from lines 6 – 19)
21       then i := i + 1;
22   end { * of while * }
23   if ((S → α., 0)
∈ L[n]) then I is accepted with weight w
24   else I is rejected;
25   end { * of Earley * }.
    
```

The Earley has the following properties:

(1) If  $(A \rightarrow \alpha \cdot \beta, i) \in L[j]$  then

$$\alpha \rightarrow \alpha_{i+1}^* \alpha_{i+2} \dots \alpha_j$$

(2) The space and time complexities to make the parse lists are  $O(n^2)$  and  $O(n^3)$ , respectively. The time complexity to create all syntactic trees of a string is  $O(c^n)$  [14].

In the following, how the parsing grammar and input string searching perform, it has been shown with an example.

Consider CFG  $G = (V_N, V_T, p, S)$  where  $V_N = \{S, T, A, B\}$ ,  $V_T = \{a, b\}$ ,  $P = \{S \rightarrow T, S \rightarrow AB, T \rightarrow aTb, T \rightarrow ab, A \rightarrow aA, A \rightarrow a, B \rightarrow bB, B \rightarrow b\}$  and  $L(G) = \{a^n b^m \mid n, m \geq 0\}$  and input string  $I = aabb$ . Fig 1 shows the procedure of described algorithm.

L[0]	(1) ( $S \rightarrow \cdot S, 0$ ) <i>initial setting</i> (2) ( $S \rightarrow \cdot T, 0$ ) <i>predict(1)</i> (3) ( $S \rightarrow \cdot AB, 0$ ) <i>predict(1)</i> (4) ( $T \rightarrow \cdot aTb, 0$ ) <i>pred(2)</i> (5) ( $T \rightarrow \cdot ab, 0$ ) <i>pred(2)</i> (6) ( $A \rightarrow \cdot aA, 0$ ) <i>pred(3)</i> (7) ( $A \rightarrow \cdot a, 0$ ) <i>pred(3)</i>
L[1]	(8) ( $T \rightarrow a \cdot Tb, 0$ ) <i>scan(4)</i> (9) ( $T \rightarrow a \cdot b, 0$ ) <i>scan(5)</i> (10) ( $A \rightarrow a \cdot A, 0$ ) <i>scan(6)</i> (11) ( $A \rightarrow a \cdot, 0$ ) <i>scan(7)</i> (12) ( $T \rightarrow aTb \cdot, 1$ ) <i>pred(8)</i> (13) ( $T \rightarrow ab \cdot, 1$ ) <i>pred(8)</i> (14) ( $A \rightarrow aA \cdot, 1$ ) <i>pred(10)</i> (15) ( $A \rightarrow a \cdot, 1$ ) <i>pred(10)</i> (16) ( $S \rightarrow A \cdot B, 0$ ) <i>complete(11,3)</i> (17) ( $B \rightarrow \cdot bB, 1$ ) <i>pred(16)</i> (18) ( $B \rightarrow \cdot b, 1$ ) <i>pred(16)</i>
L[2]	(19) ( $T \rightarrow aTb \cdot, 1$ ) <i>scan(12)</i> (20) ( $T \rightarrow a \cdot b, 1$ ) <i>scan(13)</i> (21) ( $A \rightarrow a \cdot A, 1$ ) <i>scan(14)</i> (22) ( $A \rightarrow a \cdot, 1$ ) <i>scan(15)</i> (23) ( $T \rightarrow aTb \cdot, 2$ ) <i>pred(19)</i> (24) ( $T \rightarrow ab \cdot, 2$ ) <i>pred(19)</i> (25) ( $A \rightarrow aA \cdot, 2$ ) <i>pred(21)</i> (26) ( $A \rightarrow a \cdot, 2$ ) <i>pred(21)</i> (27) ( $S \rightarrow A \cdot B, 0$ ) <i>comp(22,3)</i> (28) ( $B \rightarrow \cdot bB, 2$ ) <i>pred(27)</i> (29) ( $B \rightarrow \cdot b, 2$ ) <i>pred(27)</i>
L[3]	(30) ( $T \rightarrow ab \cdot, 1$ ) <i>scan(20)</i> (31) ( $B \rightarrow b \cdot B, 2$ ) <i>scan(28)</i> (32) ( $B \rightarrow b \cdot, 2$ ) <i>scan(29)</i> (33) ( $B \rightarrow \cdot bB, 3$ ) <i>pred(30)</i> (34) ( $B \rightarrow \cdot b, 3$ ) <i>pred(30)</i>

	(35)( $S \rightarrow AB.,0$ ) <i>comp</i> (32,27) (36)( $\$ \rightarrow S.,0$ ) <i>comp</i> (35,1) (37)( $T \rightarrow aT.b,1$ ) <i>comp</i> (30,19) (38)( $S \rightarrow T.,0$ ) <i>comp</i> (30,2) (39)( $\$ \rightarrow S.,0$ ) <i>comp</i> (38,1)
L[4]	(40)( $B \rightarrow b.B,3$ ) <i>scan</i> (32) (41)( $B \rightarrow b.,3$ ) <i>scan</i> (33) (42)( $B \rightarrow .bB,4$ ) <i>pred</i> (36) (43)( $B \rightarrow .b,4$ ) <i>pred</i> (36) (44)( $S \rightarrow AB.,0$ ) <i>comp</i> (27,37) (45)( $\$ \rightarrow S.,0$ ) <i>comp</i> (40,1) (46)( $T \rightarrow aTb.,1$ ) <i>scan</i> (37) (47)( $T \rightarrow aT.b,1$ ) <i>comp</i> (46,19) (48)( $S \rightarrow T.,0$ ) <i>comp</i> (46,2) (49)( $\$ \rightarrow S.,0$ ) <i>comp</i> (48,0)

Fig 1. Earley algorithm for l=aabb

### III. THE EARLEY ALGORITHM'S DISADVANTAGES

As it has been seen, this algorithm performs the parsing grammar and searching input string, in three steps predict, scan and completing. In order to prevent having the repeating items each time, when it expects, new item adds to the list, comparing that with all items exist at the list, happens. Also in each completing performance all items at each rows should checked out, to find the specific item and all these takes lots of time at the grammars with lots of rules and will have the very high time complexity, which will be at the  $O(n^2)$  order in the best case[5-6].

This algorithm performs, recognizing and grammar parsing in the very complicated way and takes lots of time. Another problem is using array data structure at implementing. One of the array data structure problem is the fixed length which has to be very definite from the beginning, so in order to implement the algorithm we have to consider the array bigger than usual therefore it won't having the problem when new item produces, and perform well for different grammars with the different rules, but it might lots of the

memory spaces stay vacant and waste lots of memories.

### IV. THE PROPOSED ALGORITHM

Cause of the problems have been mentioned, we introduce an algorithm which won't have most of the previous problems. In this algorithm at first in order to solve the array's problem, use of the linked list has been suggested reason for that: this data structure is flexible for the length changing during performance, also insertion and deletion of the element at linked list is doable with  $O(1)$  easily. Therefore at this algorithm we allow all the nodes to be added in the list and it won't be needed to compare anymore. Another thing about this suggested algorithm is : with the changes at the Earley's performance, would haven't been need to compare so would have been deleted lots of comparing. Suggested algorithm, does its own performance in n steps (n is the length of the input string) and maximum at each steps will produce nodes equal to the rules exist in rules set (called R) therefore  $n \cdot R$  nodes produce in order to recognize the input string, in the other way R represents the number of the repeating while( $p \neq \text{null}$ )loop. At each step three comparison happens so  $n \cdot R \cdot 3$  comparison are needed for all nodes exist at linked list .All these are less than cubic order at the Earley algorithm. Also cause using the linked list the quantity wasting memory has become zero. This algorithm won't need to completed operation. So lots of comparisons cause of completed operations will be eliminated. In order to use of the suggested algorithm shouldn't exist left-recursion in grammar. Suggested algorithm has the time complexity of the  $O(n \cdot R)$ (n is length of the input string and R is the number of rules in the rule set).fig 2 shows the proposed algorithm as described up.

```

1 new link list *p,*q;
2 p → data = ($ → .S)
3 p → next = null;
4 q = p;
5 i = 0;
6 while (i ≤ n)
7     new link list *r,*h;
8     r → data = header;//list is not
9     empty //
9     h = r;
10    While(p!=null)
11        if (p → data = ($ → α.Yβ) )
12            if (Yβ = λ)
13                if (i ≠ n)
14                    Break;
15                elseif (i == n)
16                    (print input string is accepted);
17                    else if (Y is nonterminal)
18                        if (i ≠ n)
19                            foreach(Y → ψ ∈
20                                production set){*predictor*}
21                                New node * temp;
22                                temp → data =
23                                ($ → α.ψβ)
24                                temp → next =
25                                null;
26                                q → next = temp;
27                                else if (i == n)
28                                    break;//go to line
29                                40 //
30                                else if (Y is terminal)
31                                    if (i ≠ n)
32                                        if (Y =
33                                            ai+1){*scanner*}
34                                            new node * temp;
35                                            temp → data =
36                                            ($ → αY.β);
37                                            temp → next =
38                                            null;
39                                            r → next = temp
40                                            r = temp;
41                                            else
42                                            Break;//go to line42//
43                                            else
44                                            break;
45                                            end

```

```

40    p = p → next;
41    }
42    p → next = h;
43    q = r;
44    i = i + 1;
45    }

```

Fig 2. Suggested algorithm

At the following, the example of the part 2, with getting help from the suggested algorithm, for the input string (I=aabb) has been represented. Fig 3 represents function of the suggested method.

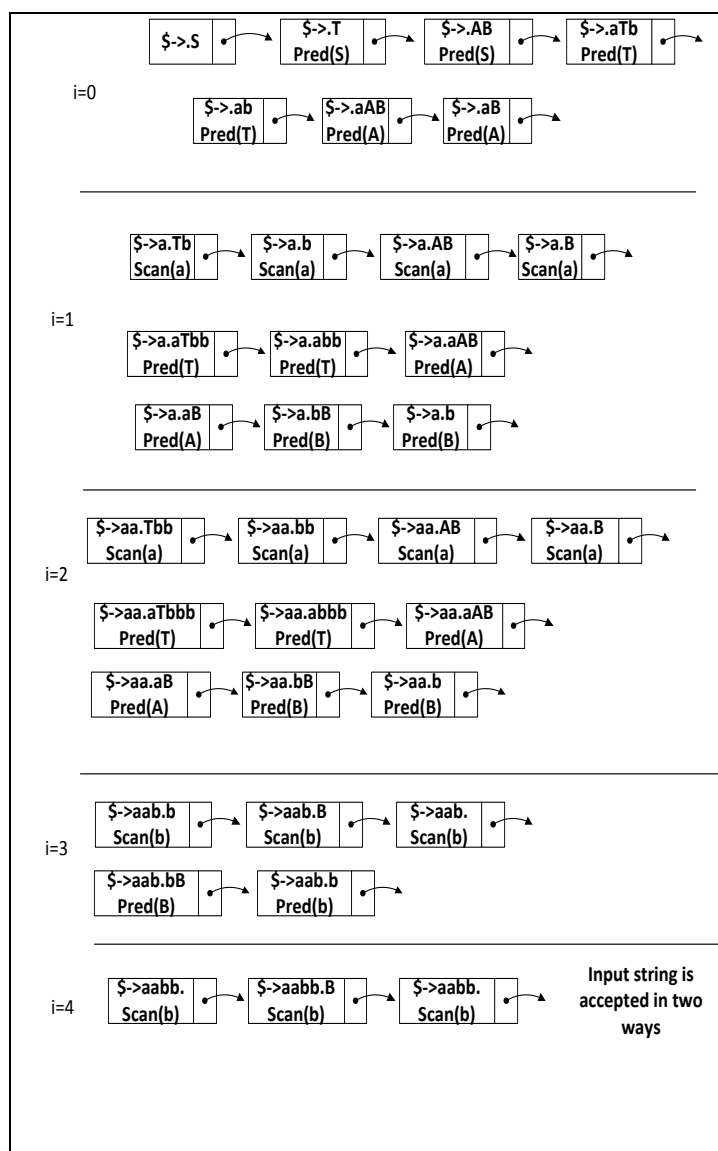


Fig.3 suggested algorithm for I=aabb

## V. CONCLUSION

At this article , At first ,we have reviewed one of the tabular parsers which has been used at recognizing syntactic pattern ,called Earley ,and then we discussed about advantages and disadvantages. Then we suggested an algorithm which decreased the cubic time complexity of the Earley algorithm to the  $O(n \cdot R)$  time complexity with using the linked list and changing at parsing performance. Also decrease the amount of wasting memory to the zero with the linked list.

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